

Task 1 - I Have, Who Has

Cluster	Reasoning with Rational Numbers
Standard(s)	<p>NC.7.NS.1 Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers, using the properties of operations, and describing real-world contexts using sums and differences.</p> <p>NC.7.NS.3 Solve real-world and mathematical problems involving the four operations with rational numbers. (NOTE: Computations with rational numbers extend the rules for manipulating fractions to complex fractions.)</p>
Materials/Link	<ul style="list-style-type: none"> • I Have, Who Has cards printed and cut apart - one per student <ul style="list-style-type: none"> ○ There are blank cards in case the teacher needs to make more so each student will have one. • Suggestion: Print on cardstock and laminate. These are good to have on hand for a quick review throughout the year.
Learning Goal	Students will apply previous learning to add and subtract positive and negative integers without the use of a calculator.

Task overview

Students will be playing the game I Have, Who Has

Prior to lesson

- Students will have learned to add and subtract positive and negative integers

Teaching Notes

Task Launch:

Give the students the following and allow them to work in pairs to come up with as many solutions as possible.

Directions: Using the numbers 1 to 9 at most once each time, fill in the blanks to make the statement true:

___ and ___ are ___ units away from ___

(one possible solution 3 and 7 are 2 units away from 5)

Directions:

- Explain the rules of the game to students. Tell them this is a mental math exercise and they should respect wait time.
- Give every student at least one card. If necessary, some students may have more than one card. All cards must be distributed.
- Choose one student to start. They will read the "Who has" part of the card.
- The student with the answer must respond I Have _____, then read the "Who has" part of his/her card.
- This continues until the first student answers with the I Have part of his/her card.

Suggestion

You may want to have each student keep a running total on a piece of paper or on a white-board to monitor engagement.

I Have ... Who Has ...

I Have -10	Who has my number in- creased by 3	I Have -7	Who has my number de- creased by 5
I Have -12	Who has my number plus -8	I Have -20	Who has my number minus -4
I Have -16	Who has my number plus 20	I Have 4	Who has my number plus -30
I Have -26	Who has my number plus -2	I Have -28	Who has my number minus -13
I Have -15	Who has my number minus 8	I Have -23	Who has my number plus 30
I Have 7	Who has my number plus -5	I Have 2	Who has my number plus -21
I Have -19	Who has my number minus 8	I Have -27	Who has my number minus -13
I Have -14	Who has my number plus -16	I Have -30	Who has my number in- creased by 30

I Have 0	Who has my number de- creased by 50	I Have -50	Who has my number in- creased by 60
I Have 10	Who has my number in- creased by 15	I Have 25	Who has my number plus -20
I Have 5	Who has my number plus 17	I Have 22	Who has my number plus 22
I Have 44	Who has my number minus -6	I Have 50	Who has my number plus 10
I Have 60	Who has my number de- creased by 20	I Have 40	Who has my number plus -14
I Have 26	Who has my number minus 27	I Have -1	Who has my number plus 13
I Have 12	Who has my number plus -22	I Have	Who Has
I Have	Who Has	I Have	Who Has

Task 2 - The Integer Product Game	
Cluster	Reasoning with Rational Numbers
Standard(s)	NC.7.NS.3 Solve real-world and mathematical problems involving the four operations with rational numbers. (NOTE: Computations with rational numbers extend the rules for manipulating fractions to complex fractions.)
Materials/Link	<p>Each pair of students needs:</p> <ul style="list-style-type: none"> • One game board • Two paper clips • Colored markers or chips (2 colors) <p>Suggestion: Print game boards on cardstock and laminate. These are good to have on hand for a quick review throughout the year.</p> <p>If digital devices are available, students can play online here: http://media.pearsoncmg.com/curriculum/math/cmp3/activities/A82388/index.html</p>
Learning Goal	<ul style="list-style-type: none"> • Students will apply multiplication and division algorithms in the Integer Product Game.
<p>Task overview</p> <p>Students will play the Integer Product Game either online or on paper. The game requires students to multiply and divide positive and negative integers and have an understanding of factors.</p>	
<p>Prior to lesson</p> <ul style="list-style-type: none"> • Students have developed algorithms for adding, subtracting, multiplying, and dividing integers. 	
<p>Teaching Notes</p> <p>Task Launch: Give the students the following and allow them to work in pairs to come up with as many solutions as possible.</p> <p>Using the numbers 1 to 9 at most once each time, fill in the blanks to make the equality true:</p> $(_ + _ - _ + _) - (_ + _ - _ + _) = 0$ <p>Directions:</p> <ul style="list-style-type: none"> • Explain the rules of the game. • Allow students to play several rounds of the game. • Encourage them to look for strategies for picking factors and products. 	

- Have students answer the questions on the student sheets.
- Allow time for students to share their responses, particularly about strategies used.
- If there is time, allow students to play more rounds of the game.

Rules

1. Player A puts a paperclip on a number in the factor list.
2. Player B puts the other paper clip on any number in the factor list, including the number chosen by Player A. Player B then marks the product of the two factors on the product grid.
3. Player A moves either one of the paper clips to another number. He or she then marks the new product with a different color than Player B.
4. Each player takes turns moving a paper clip and marking a product. A product can only be marked by one player.
5. The winner is the first player to mark four squares in a row (up and down, across, or diagonally).
 - a. What product would give the least number?
 - b. What product would give the greatest number?

Student materials below

The Integer Product Game

-36	-30	-25	-24	-20	-18
-16	-15	-12	-10	-9	-8
-6	-5	-4	-3	-2	-1
1	2	3	4	5	6
8	9	10	12	15	16
18	20	24	25	30	36

-6 -5 -4 -3 -2 -1 1 2 3 4 5 6

The Integer Product Game

Play the Integer Product Game with positive and negative factors. Look for strategies for picking the factors and products.

- A. What strategies did you find useful in playing the game? Explain.
- B. What pair(s) of numbers from the factor list will give each product?
- 5
 - 12
 - 12
 - 25
- C. Your opponent puts a paper clip on -4 . List five products that you can form, assuming they are not marked. Tell where you would need to put your paper clip in each case.
- D. Describe the moves to make in each case.
- The paper clips are on -5 and -2 . You want a product of -15 .
 - The paper clips are on -3 and -2 . You want a product of -6 .
 - Your opponent will win with 24. What numbers should you avoid with your paper clip moves?
- E. Mia thinks the game could also be called the Division Game. Explain why Mia might think this.

Anticipated responses/strategies:

Part A

- Even products have more factors
- Signs really don't matter in selecting factors
- If my partner made an positive product, I tried to make a negative in the beginning and vice versa
- If my partner made an odd product, I tried to make and even and vice versa
- I tried to start with a product that had the most factors

Part B

- 1,5 and -1,-5
- -2, 6 and 2, -6 and -3,4 and 3, -4
- 2,6 and -2,-6 and -3,-4 and 3,4
- -5,-5

Part C

Times -4	Product
-6	24
-5	20
-4	16
-3	12
-2	8
-1	4

Times -4	Product
6	-24
5	-20
4	-16
3	-12
2	-8
1	-4

Watch for students signing incorrectly

Part D

- Move the clip to 3
- Move the clip on -3 to 3 or move the clip from -2 to 2
- 6,4,3,-6,-4,-3 - They are factors of 24

Task 3 - Tasks Around the Room

Cluster	Reasoning with Rational Numbers
Standard(s)	NC.7.NS.3 Solve real-world and mathematical problems involving the four operations with rational numbers. (NOTE: Computations with rational numbers extend the rules for manipulating fractions to complex fractions.)
Materials/Link	<ul style="list-style-type: none"> • Task cards printed, cut apart and numbered • Clipboards (one per student) or student notebooks, whichever is least cumbersome and easy to carry around the room • Suggestion: Print on cardstock and laminate. These are good to have on hand for a quick review throughout the year.
Learning Goal	<ul style="list-style-type: none"> • Students will solve real-world mathematical problems involving the four operations with rational numbers.

Task overview

The students will travel around the room solving various tasks. The tasks require students to write a numerical expression and solve using all four operations with rational numbers.

Prior to lesson

- Students have developed algorithms for adding, subtracting, multiplying and dividing rational numbers.

Teaching Notes

Task Launch:

Give the students the following and allow them to work in pairs to come up with as many solutions as possible.

Directions: Using the numbers -5 to 5 at most once each, write an expression that will have the greatest (or least) absolute value.

$$\frac{\square}{\square} (\square - \square) - \square (\square - \square)$$

Directions:

- Before students arrive, place the task cards in various locations around the room. If possible, leave enough space for students to work.
- Students can work individually or in pairs.
- Explain to students there are various tasks located around the room. They will be moving around the room to solve.
- Students should solve the task on their own paper or in notebooks (teacher preference).
- Assign students a number to start with and tell them to move sequentially. For example, if a student begins with #14, they will move to #15 next. This should help keep too many students from being at the same card at once.
- Monitor students to ensure they are creating numerical expressions that represent the problem accurately.

Student materials below

<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>The temperature rose 13°F between noon and 5:00 p.m. and then fell 7°F from 5:00 p.m. to 10:00 p.m. If the temperature at noon is 75°F, what would the temperature be at 10:00 p.m.?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Paola was standing on top of a cliff 35 feet above sea level. She watched her friend Juan jump from the cliff to a depth of 12 feet into the water. How far apart are the two friends?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Eli left school and walked 5 blocks south. Chloe left school and walked the same distance north. How far apart did the two friends end up?</p>
<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Daniel and his mother flew from Miami, Florida to Maine to visit family. When they left Miami, the temperature was 84°. When they arrived in Maine it was -7°. What was the temperature change Daniel and his mother?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>The Panthers got possession of the football on their own 35 yard line. They ran for an 8 yard gain. The next play was a 13 yard loss. What is their field position after the two plays?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Caroline has \$85 in her bank account. After she went shopping, she looked at her account again and she had $-\\$16$. How much did she spend shopping?</p>
<p>Write a story problem you could model with positive and negative numbers, then model and solve.</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Mr. Jenkins lives in Michigan. When he leaves for work one wintry morning, the temperature is -4°C. By the time he comes home, the temperature has increased 25°. What is the temperature when he comes home?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Sam borrowed \$7 from his brother every week for 5 weeks. What is Sam's financial situation with his brother at the end of the 5 weeks?</p>

<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Erika borrowed \$5 each from 6 different friends. How much money does Erika owe her friends altogether?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>The temperature decreased 2° per hour for six hours. How many degrees did the temperature decrease after six hours?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>During a shark week special, a diver descended 2.5 feet every minute. How many feet will he descend in 10 minutes?</p>
<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>During a trivia contest, a team receives 50 points for every correct answer and loses 45 points every time they get a question incorrect. After a new game of 30 questions, the team misses 16 questions. How many points did they have at the end of the game?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>An oven temperature dropped 225° in 25 minutes. If the temperature dropped at a constant rate, how many degrees per minute did the temperature drop?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>You are playing Fortnite and you have 75 wood, 29 brick and 34 metal. It takes 10 of each material to build a wall. You can't mix materials in building a wall. How many walls can you build?</p>
<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Tracy is ordering a new pair of eyeglasses. The frames she wants cost \$88.70. Transition lenses cost \$78.00. Her insurance says that they will pay \$100 of the cost, and 20% of the remaining amount. How much will Tracy have to pay?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Amanda wants to run 26.2 miles, the distance of a marathon, in a month. She plans to run $\frac{3}{4}$ of a mile each day. How many days will she need to run? Will she be able to reach her goal?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Matthew is working for the city maintenance department. He will be painting railings throughout town. He gets paid \$0.60 for every foot of railing that he paints. If Matthew paints an average of 45 yards of railing a week, how much can he earn in $9\frac{3}{5}$ weeks?</p>

<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>A deep freezer can change the internal temperature of a 12 pound roast by -1.8° F every 10 minutes. How much will the temperature of the roast change in $2\frac{3}{4}$ hours?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Chip is ordering 5 dozen donuts for his wife's birthday party. He wants $\frac{1}{4}$ of the donuts to be glazed with chocolate frosting and sprinkles, and $\frac{1}{3}$ of the donuts to have cream filling. The rest of the donuts will be plain glazed. The plain glazed donuts cost \$0.17 each, and the other donuts cost \$0.28 each. How much will Chip have to pay for all the donuts?</p>	<p>Write a numerical expression that models your solution and then write a complete sentence stating your answer.</p> <p>Leslie wants to buy new carpet for her bedroom. She measured the dimensions of her bedroom and found that it was $14\frac{3}{4}$ feet by $11\frac{5}{8}$ feet. Installation will cost \$63.50. If Leslie wants to spend no more than \$800 on carpet, including installation, how much can she afford to pay for each square foot?</p>
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Anticipated strategies/responses:

$75 + 13 - 7$ or $75 + 13 + (-7)$ The temperature at 10:00 pm is 81 degrees.	$35 - (-12)$ or $35 + 12$ The friends are 37 feet apart.	$5 - (-5)$ or $5 + 5$ The friends are 10 blocks apart.
$84 - (-7)$ or $-7 - 84$ The temperature dropped 91 degrees. Students may have trouble interpreting the -91 vs the 91	$35 + 8 + (-13)$ or $35 + 8 - 13$ or $35 - 5$ or $35 + (-5)$ The panthers are at the 30 yard line.	$85 - (-16)$ Caroline spent \$101. Incorrect: $85 - 16$ or $85 + -16$
Answers will vary	$-4 + 25$ The temperature is 21 degrees.	-7×5 or $-7 + -7 + -7 + -7 + -7$ Same owes his brother \$35. Some students may do 7×5 with the understanding same would be in debt \$35
-5×6 or $-6 + -6 + -6 + -6 + -6 + -6$ Erika owes \$30 total. Some students may do 5×6 with the understanding same would be in debt \$30	$26.2 \frac{3}{4}$ or $26.2 0.75$ It will take her 35 days to get all the miles in. She can't do that because there is not a month with 35 days. Some students may not know how to interpret the answer 34.93333....	$45 \times 3 \times 0.60 \times 935$ $45 \times 3 \times 0.60 \times 9.6$ Matthew will make \$777.60.
$-1.8 \times (2 \frac{3}{4} 16)$ $-1.8 \times (2.75 16)$ $-1.8 \times (165 10)$ The roast temperature will drop about 29.7 degrees. Some students may think the 12 needs to be used and multiply by it as well.	$14 (60)(.28) + \frac{1}{3} (60)(.28) + 512(60)(.17)$ The donuts will cost \$14.05. Some students may try to make all fractions decimals. Some may figure out the number of donuts and mentally. Ex. $\frac{1}{3}$ of 60 is 20 Some students may use 5 in the equation instead of 60.	$(800 - 63.50) (14 34 \times 11 58)$ Leslie can pay about \$4.29 per square foot. Students may forget parenthesis. They may also use one form of all numbers ex .all decimals or fractions. Students may struggle with interpreting the partial square feet.